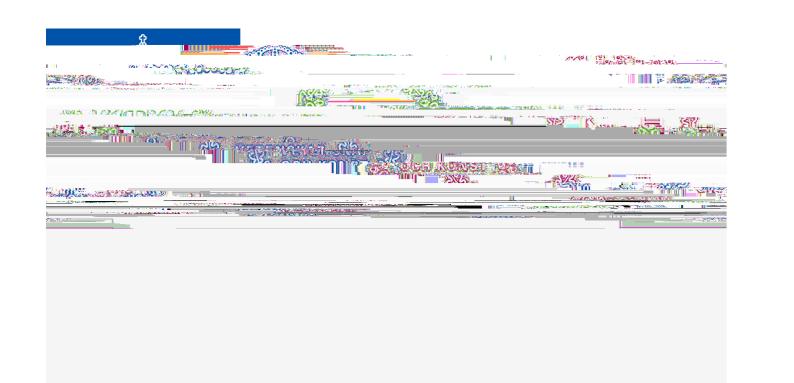
## Gap probabilities in piecewise thinned Airy and Bessel point processes



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Based on several works with T. Claeys and A. Doeraene

## Gap in the piecewise thinned Airy point process

The Airy point process is a determinantal point process on R, arising near soft edges of certain large random matrices.

Let  $m \ge N_{>0}$ ,  $s = (s_1; ...; s_m) \ge [0; 1]^m$  and  $x = (x_1; ...; x_m) \ge R^m$  be such that  $1 < x_m < ... < x_1 < x_0 = +1$ .

For  $j \ge f(1;2; :::; mg)$ , each particle on the interval  $(x_j; x_{j-1})$  is removed with probability  $s_j$ .

We consider the probability to observe a gap on  $(x_{m'} + 7)$  in the thinned process. This probability can be written as a Fredholm determinant:

$$F(X; S) = \det 1 \qquad (x_{m, + 1}) \qquad (1 \qquad S_j) K^{Ai} \qquad (x_{j, x_{j-1}}) \qquad : j = 1$$

## Exact expression for F(x; s) and a system of Painlevé II equations

If m = 1, Tracy and Widom ('94) have shown that F(x; s) can be expressed in terms of a solution to a Painlevé II equation. This result was generalised by Claeys-Doeraene ('18) for an arbitrary m = 1 as follows

$$F(X; S) = \exp_{\substack{i=1 \\ j=1 \\ 0}} \exp_{\substack{j=1 \\ 0}} q_j^2(; X; S) d;$$

where  $q_1, \ldots, q_m$  satisfy a system of *m* coupled Painlevé II equations

$$q_{j}^{\mathcal{M}} = (+x_{j})q_{j} + 2q_{j} \qquad q_{j}^{2}; \qquad j = 1; ...; m;$$
  
$$q_{j}(; x; s) = \Pr \frac{\sum_{j=1}^{j=1} (+x_{j})(1 + o(1));}{s_{j+1} \qquad s_{j}^{2} \operatorname{Ai}(+x_{j})(1 + o(1));} \qquad \text{as} \qquad l = 1, ..., m;$$

where  $S_{m+1} := 1$ .